# Humidity profile retrieval with the Clermont-Ferrand VHF wind profiler V. Klaus<sup>(1)</sup>, J. Van Baelen<sup>(2)</sup>, and Y. Pointin<sup>(2)</sup>

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Abstract

The humidity profile can be derived from ST radars echo power and spectral width, provided the temperature profile, and one at least one humidity reference (either integrated or at a given altitude within the radar altitude range), are known. This technique has already been successfully implemented on VHF [3] [8] [12], and UHF radars [7]. To this purpose, several algorithms have been developed, as presented for example in [5], and [12].

In this project, we will use the particular topography of the Puy-de-Dôme Observatory to our advantage. The Laboratoire de Météorologie Physique (LaMP) Clermont-Ferrand VHF profiler is located a few kilometres from the Puy de Dôme, which culminates at an altitude close to the first range gate of the radar (1464 m). At its summit, continuous measurements are performed with a humidity sensor and a GPS station, which provides the integrated water vapour (IWV).

Hence, we will be able to test the different humidity profile retrieval approaches, and particularly the direct exploitation of the IVW data without the need of any assumption on the vertical distribution of the water vapour. This information, completed by reference data at the top (negligible humidity near the tropopause) and at the base of the profile (humidity sensor data) will give us a unique opportunity to fine-tune the retrieval algorithm and to cross check the measurement quality.

Finally, the humidity profiles retrieved with the VHF profiler will be validated by comparisons with the LaMP newly acquired water vapour Raman lidar.

#### 1.Theoretical background

#### 1.1 radar turbulence data: $\eta$ and $\varepsilon$

Two main algorithms have been used to extract humidity gradients from the wind profiler data (WPR). The first one uses the refractive index gradient *M* [12], the second one the potential refractive index  $\phi$  [11]. Both require the reflectivity and the turbulent dissipation rate values calculated respectively from the zeroth and the second moment of the radar signal on the spectrum.

Reflectivity  $\eta$  retrieval can be directly obtained from the signal-to-noise ratio of the radar spectral signal, using for example the classical equation [13]:

$$\eta = \frac{9\pi}{2} \frac{ckB\left(T_c + \frac{T_{rx}}{\alpha}\right)}{\alpha P_t F_r A_e \cos\beta} \left(\frac{z}{\Delta z}\right) \left(\frac{S}{N}\right)$$
(1)

Where:

 $T_{rx}$  = Receiver noise temperature

 $\alpha$  = Efficiency of the antenna and transmission line

 $P_t$  = Peak transmitted power

 $F_r$  = Pulse repetition frequency

 $A_{p}$  = Effective antenna area

*b* = Antenna beam elevation angle

Dz = Range resolution

S/N = Signal-to-noise ratio

with:

c = velocity of light k = Boltzmann's constant

 $T_c$  = Cosmic noise temperature

The turbulence dissipation rate  $\varepsilon$  is deduced from the the spectral width  $\sigma$  after corrections due to wind shears and other contributions as described in [14]: being successfully tested by comparison with in-situ measurements [6]:

$$\varepsilon = \sigma_t^2 \left( \frac{4\pi}{A} \right)^{\frac{3}{2}} J^{-\frac{3}{2}}$$
 (2)

with: (3)

$$J = 12 \Gamma\left(\frac{2}{3}\right) \int_0^{\frac{r}{2}} \sin^3 \phi \int_0^{\frac{r}{2}} \left[ b^2 \cos^2 \phi + a^2 \sin^2 \phi + \left(\frac{L^2}{12}\right) \sin^2 \phi \cos^2 \theta \right]^{\frac{1}{3}} d\theta \, d\phi$$

where:

 $s_{t}$  = Spectral width due to turbulence, corrected from wind shear and other factors

A = 1.53 to 1.68 (see [14])

G = Gamma function

L = the product of the mean wind speed and the Doppler time series duration

$$a = \frac{r\theta}{4\sqrt{\ln 2}} \quad (4) \qquad \qquad b = \frac{h}{4\sqrt{\ln 2}} \quad (5)$$

r = range, q = elevation angle, h = pulse length

# 1.2 humidity equation

*M* is estimated from the general equation:

$$M = -77,6x10^{-6} \cdot \frac{P}{T} \left[ \frac{N^2}{g} \left( 1 + 15600 \frac{q}{T} \right) - \frac{7800}{T} \frac{dq}{dz} \right] \quad (6)$$

Giving:

$$\frac{dq}{dz} - \left(\frac{2N^2}{g}\right)q = 1,652\frac{T^2}{P}M + \frac{T}{7800}\frac{N^2}{g} \qquad (7)$$

$$N^{2} = g \cdot \frac{dT}{dz} = \frac{3}{T} \cdot \left( \frac{dT}{dz} + \Gamma \right)$$
(8)  
$$q(z) = 1,652\theta^{2} \int_{z0}^{z} \frac{T^{2}M}{P\theta^{2}} dz + \frac{\theta^{2}}{7800g} \int_{z0}^{z} \frac{TN^{2}}{\theta^{2}} dz + \theta^{2} \frac{q_{0}}{\theta^{2}}$$
(9)

With:  $\theta$  = Potential temperature,

T = Absolute temperature,

P = Atmospheric pressure,

g = Acceleration of gravity,

 $q_0$  and  $\theta_0$  = Respectively humidity and potential temperature at the boundary height

For further developments, Eq (9) will be written as:  $q(z) = a_0(z) + b_0(z) + c_0(z)q_0$ (10)with:

$$a_{0}(z) = 1,652 \theta^{2} \Big|_{z0}^{z} \frac{T^{2}M}{P\theta^{2}} dz$$
 (11)

$$b_0(z) = \frac{\theta^2}{7800 g} \int_{z_0}^{z} \frac{T N^2}{\theta^2} dz$$
 (12)

$$c_0(z) = \frac{\theta^2}{\theta_0^2} \tag{13}$$

Eq (8) directly provides the  $N^2$  profile. Then  $\theta$  profile is

calculated by integrating  $N^2$ :  $\theta(z) = \theta_0 e^{\int_{z_0}^{z} \frac{N^2(x)}{g} dx}$ with

$$\theta_0 = \tau_0 \left( \frac{1000}{P_0} \right)^{\frac{Ra}{Cpa}}$$
. P is deduced from  $P = P_0 \left( \frac{\tau}{\tau_0} \right)^{\frac{Cpa}{Ra}}$ 

The humidity equation can thus be solved if only M and T profiles, ground pressure and temperature, and humidity at a given range or over a larger layer are known.

(15)

The last parameter *M* is provided by the radar:

From [7] 
$$|M| = K L_0^{-\frac{2}{3}} \eta^{\frac{1}{2}}$$
 (14)  
From [1]:  $|M| = K' F^{\frac{1}{2}} N \varepsilon^{-\frac{1}{3}} \eta^{\frac{1}{2}}$  (15)

With:

 $L_0$  = Outer scale of turbulence F = Filling factor of turbulence

In this process, attention should be paid to the sign ambiguity of M, because statistically, M can become positive in 10 to 20% of cases. This ambiguity can be solved in a first approximation if we notice that generally M becomes positive when  $N^2$  is below a certain threshold of few 10<sup>-5</sup> rad<sup>2</sup> s<sup>-2</sup> [12]

The other algorithm [11], not described here due to lack of space, could be used, replacing M with the potential refractive index  $\varphi$ , bringing he same form of equation as Eq (10)

#### Algorithm implementation 2.

#### 2.1 One humidity reference point

Theoretically, only one humidity reference must be

known in order to solve the equation. For a VHF radar reaching at least the upper troposphere, this condition is easily met, assuming negligible humidity at 9 km height for example.

$$q(zi) = a_0(zi) + b_0(zi) + c_0(zi)q_0$$
(16)

From (16), q0 is deduced, allowing the direct resolution of (10)

## 2.2 Two humidity reference data

As already mentioned by Tsuda et al. [1], the radarderived value of *M* may differ from the true one by a proportion coefficient. Moreover, calibration data may not always be much accurate or may change with time. Consequently, another unknown parameter K should be introduced in the term of *M*, changing (10) into:

$$q(z) = K.a_0(z) + b_0(z) + c_0(z)q_0$$
(17)

For example, information on total humidity value qt would give us the extra parameter needed to solve (10). In that case, we would have the couple of two two equation with 2 unknowns (K and q0):

$$q(zi) = K.a_0(zi) + b_0(zi) + c_0(zi)q_0$$
  

$$qt = K.A_0 + B_0 + C_0 q_0$$
(18)

With A<sub>0</sub>, B<sub>0</sub>, and C<sub>0</sub>, being the integrated value of a<sub>0</sub>, b<sub>0</sub>, and c<sub>0</sub>, respectively over the whole range of the profile.

The GPS instrument could provide the integrated water vapour (IWV) from the ground up to the satellite. It has been demonstrated that total humidity inside the radar range could be accurately estimated from previous radio soundings [8] or other other remotesensing devices such as radiometer.

## 2.3 Three humidity reference data

In equations (14) and (15),  $L_0$  and F are supposed to be constant with altitude. This assumption, already discussed [1], may involve non negligible errors as several studies have shown large height variations of  $L_0$  even in the lower troposphere [2][9].

Consequently, a further variable K, should be introduced to express, at least at first approximation, the height variations which may occur for each profiling. The general humidity equation (17) thus becomes:

$$q(z) = (K + K'z) \cdot a_0(z) + b_0(z) + c_0(z)q_0$$
(19)

In this case a third humidity reference would be necessary, for example, the value at a given height zj. This provides us with a new system of 3 equation for three unknown to solve (q0, K and K'):

$$q(zi) = (K + K'z) a_0(zi) + b_0(zi) + c_0(zi) q_0$$
  

$$q(zj) = (K + K'z) a_0(zj) + b_0(zj) + c_0(zj) q_0$$
  

$$qt = K.A_0 + K'.A'_0 + B_0 + C_0 q_0$$
(20)

With  $A'_{o}$  being the integrated value of  $(z.a_{o})$ ,) over the whole range of the profile.

Eq (20) needs to be solved before calculating the q profile from the equation (19).

### 3. Simulation with radio soundings

The two-month Mesoscale Alpine Project (MAP) Campaign in the region of Milan (Italy) [1] was used to test this technique. A large number of controlled measurements from the CNRM VHF radar were available and completed with nearly one hundred radio soundings launched in the vicinity.

The VHF radar belongs to the INSU/Meteo series [10], with only slight differences between the LaMP radar and the CNRM one which participated to the MAP Experiment, The characteristics are listed on the following table.

| Ta | ble: | Main | charact | teristics | s of the | VHF | <sup>-</sup> radar |
|----|------|------|---------|-----------|----------|-----|--------------------|
|----|------|------|---------|-----------|----------|-----|--------------------|

|                         | LaMP              | CNRM       |  |  |
|-------------------------|-------------------|------------|--|--|
| Frequency               | 45 MHz            |            |  |  |
| Antenna type:           | Coaxial collinear |            |  |  |
| Antenna area:           | 65x65m            | 85x130m    |  |  |
| Beamwidth:              | 5.6°              | 4.3° - 2.8 |  |  |
| Number of beams         | 5                 |            |  |  |
| Peak power:             | 5 kW              | 12 kW      |  |  |
| Pulse repetition period | 156.25 µs         |            |  |  |
| Pulse width             | 10 µs (8 codes)   |            |  |  |
| Height resolution       | 375 m             |            |  |  |
| Nbr of spectral points  | 256               |            |  |  |
| Coherent integrations   | 128               |            |  |  |
| Incoherent integrations | 7                 |            |  |  |

When the only reference point is a negligible humidity at 9 km height, the standard deviation (StD) from RS data largely extends over 1 g/kg below 5 km (Fig. 1)



Figure.1 - Left: Standard deviation between radiosonde (RS) humidity measurements and VHF radar using zero humidity reference point at 9 km height. Right: Typical example of humidity profiles obtained with RS and VHF.

The results are much better when the total humidity reference value is added, in which case, 1g/kg StD is reached only below 3 km height (Fig. 2).



Figure.2 - Same as Fig. 1 using the total humidity inside the radar range as a second reference

A third reference point value at the base of the radar range (3 km in our example) considerably improves the statistics as shown on Fig. 3.



Figure.3 - Same as Fig. 2 using a known value at 3 km height as a third reference.

These preliminary results were very encouraging for implementing a three-reference humidity system at LaMP.

#### 4. The LaMP project

### 4.1 The experimental set-up

The Puy-de-Dôme Observatory has the unique capability to implement the three humidity reference system due to the fact the Laboratoire de Météorologie Physique (LaMP) Clermont-Ferrand VHF profiler is located a few kilometres from the Puy de Dôme, which culminates at an altitude close to the first range gate of the radar (1464 m). At its summit, continuous measurements are performed with a humidity sensor and a GPS station, which provides the integrated water vapour (IWV) corresponding practically to the range covered by the radar.

#### Puy de Dôme 1464m: GPS station



Figure 4- The instrumental set-up at LaMP Hence, we will be able to test the different humidity

profile retrieval approaches, and particularly the direct exploitation of the IVW data without the need of any assumption on the vertical distribution of the water vapour.

Finally, the humidity profiles retrieved with the VHF profiler will be validated by comparisons with the LaMP newly acquired water vapour Raman lidar.

This system, along with updated radar hardware, will be fully operational at the end of 2009 for a continuous operational profiling of wind and humidity.

#### 4.2 Preliminary results

Preliminary experiment was made between 5 November and 7 December 2004 with the LaMP VHF radar completed with GPS IWV data and ground station measurements at Puy-de-Dome. At this time, the temperature profile was deduced from the standard value calculated from ground level measurements. Fig. 5 gives a synoptic view of the humidity evolution over the radar during the first week of experiment.



Figure.5 - Evolution of humidity profile over the LaMP radar site during the 2004 experiment using the GPS and ground data at Puy de Dôme with the 3 reference point method.

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#### REFERENCES

[1] Bougeault, P., P. Binder, A. Buzzi, R. Dirks, R. Houze, J. Kuettner, R. B. Smith, R. Steinacker, H. Volkert. et al.: The MAP Special Observing Period. Bull. Amer. Meteor. Soc., 82, 433-462, 2001.

[2] Eaton, F. D., and G. D. Nastrom, 1998: Profile estimates of turbulent inner and outer scales from VHF radar observations at White Sands Missile Range, NM. 4th International Symposium on Tropospheric Profiling, **1**, 88-90. [3] Furumoto, J., K. Kurimoto, and T. Tsuda, 2003: Continuous Observations of Humidity Profiles with the MU Rada-Rass Combined with GPS and Radiosonde Measurements. *J. Atmos. Oceanic Technol.*, **20**, 23-41.

[4] Gage, K. S. and B. B. Balsley, 1980: On the scattering and reflection mechanisms contributing to clear air radar echoes from troposphere, stratosphere and mesosphere. *Radio Sci.*, **15**, 243-257.

[5] Gossard, E. E. and R. G. Strauch, 1983: *Radar Observations of Clear Air and Clouds*. Elsevier, 280 pp Author3 X. Y., Z. Author4, 2007: Journal Article Title 2, *Journal Name*, **10**, pp. 25-30.

[6] Jacoby-Koaly, S., B. Campistron, S. Bernard, B. Bénech, F. Ardhuin-Girard, J. Dessens, E. Dupont, and B. Carissimo, 2002: Turbulent Dissipation Rate in the Boundary Layer via UHF Wind Profiler Doppler Spectral Width Measurements. *Boundary-Layer Meteor.*, **103**, 361-389.

[7] Klaus, V., L. Bianco, C. Gaffard, and T. Hewison, 2006: Combining UHF radar wind profiler and microwave radiometer for the estimation of atmospheric humidity profiles. *Meteor. Zeitsch.*, **15**, 87-97.

[8] Mohan, K., D. N. Rao, T. N. Rao, and S. Raghavan, 2001: Estimation of temperature and humidity from MST radar observations. *Ann. Geophysicae*, **19**, 855-861.

[9] Muschinski, A., 1997: Turbulence and gravity waves in the vicinity of a midtropospheric warm front: A case study using VHF echo-intensity measurements and radiosonde data. *Radio Sci.*, **32**, 1161-1178.

[10] Petitdidier, M., V. Klaus, C. Niangoran, M. Massebeuf, and A. Petitpa, 1990: Some aspects of horizontal wind measurements with a strato-tropospheric radar. *Meteor. Rdsch.*, **42**, 174-180.

[11] Stankov, B. B., E. E. Gossard, B. L. Weber, R. J. Lataitis, A. B. White, D. E. Wolfe, and D. C. Welsh, 2003: Humidity Gradient Profiles from Wind Profiling Radars Using the NOAA/ETL Advanced Signal Processing System (SPS). *J. Atmos. Oceanic Technol.*, **20**, 3-22.

[12] Tsuda, T., M. Miyamoto, and J. Furumoto, 2001: Estimation of a Humidity Profile Using Turbulence Echo Characteristics. *J. Atmos. Ocean. Technol.*, **18**, 1214-1222.

[13] VanZandt, T. E., J. L. Green, K. S. Gage, and W. L. Clark, 1978: Vertical profiles of refractivity turbulence structure constant: Comparison of observation by the Sunset radar with a new theoretical model. *Radio Sci.*, **13**, 819-829

[14] White, A. B., R. J. Lataitis, and R. S. Lawrence, 1999: Space and Time Filtering of Remotely Sensed Velocity Turbulence. *J. Atmos. Ocean. Technol.*, **16**, 1967-1972.